



Sustainable Energy
**Mod. 6: Fuel Cells & Distributed
Generation Systems**

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Exercise V: microturbines (calculations)

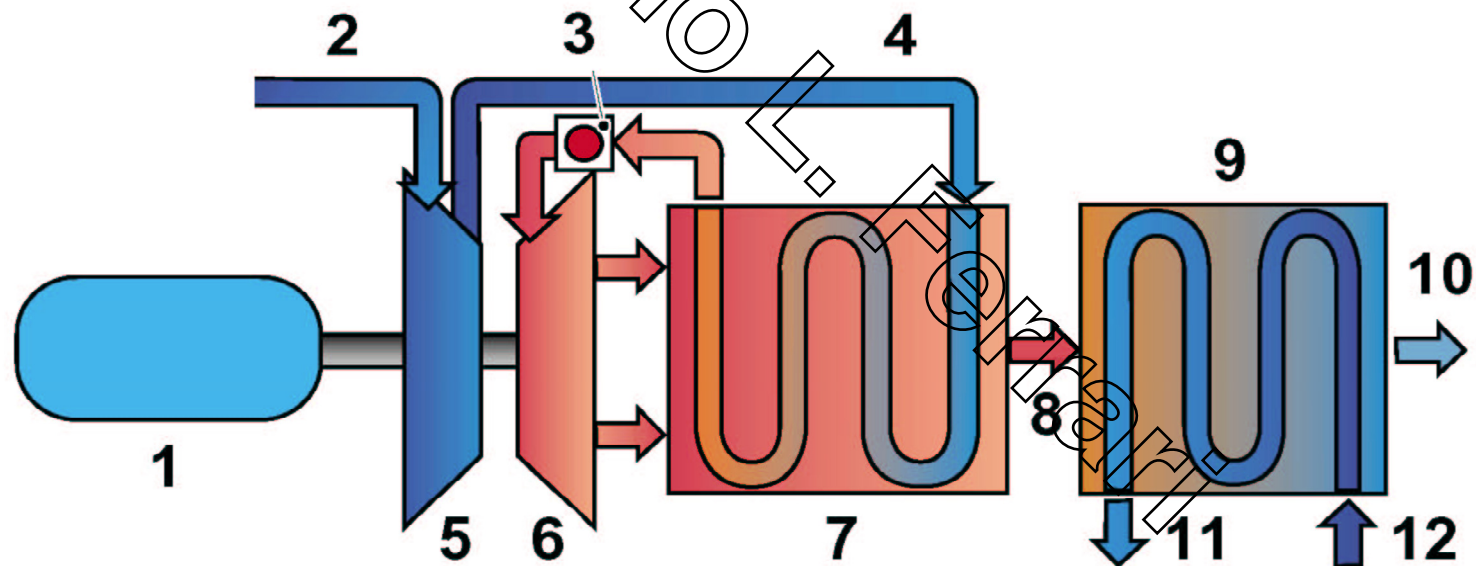
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Exercise 1: Calculate electrical and total efficiency for the T100 machine with the following data:

- **Ambient condition: 15°C, 1.013 bar ($p_4=p_1$)**
- **Air mass flow rate: 0.8 kg/s**
- **Compression ratio: 4.5**
- **Compressor efficiency: 0.72**
- **Recuperator effectiveness: 0.88**
- **Compressor-turbine pressure loss: 6%**
- **Combustion efficiency: 0.995**
- **Fuel LHV: 48000 kJ/kg**
- **Expander efficiency: 0.82**
- **TOT: 645°C**
- **Mechanical efficiency: 0.99**
- **Electrical efficiency: 0.96**
- **Auxiliary power: 7.4 kW**
- **Water outlet temperature: 95°C**
- **Water-Exhaust temp. difference - efficiency: 20°C – 0.95**

Plant layout:

Legend: 1. Generator; 2. Inlet air; 3. Combustion chamber; 4. Air to recuperator; 5. Compressor; 6. Turbine; 7. Recuperator; 8. Exhaust gases; 9. Exhaust gas heat exchanger; 10. Exhaust gas



Solution (1/2):

1. Assumption: air $c_{p_a} = 1.014 \text{ kJ/kgK}$ (so: $k_c = 1.39$)
2. Compressor outlet temperature: $T_2 = T_1 + (1/\eta_c) * T_1 * (\beta_c^{\theta_c} - 1) = 498.29 \text{ K}$
3. Compressor outlet pressure: $p_2 = p_1 * \beta_c = 4.56 \text{ bar}$
4. Calculation of compressor power: $P_c = m_a * c_{p_a} * (T_2 - T_1) = 170.47 \text{ kW}$
5. Combustor inlet temperature: $T_5 = (T_4 - T_2) * \epsilon + T_2 = 867.77 \text{ K}$
6. Turbine inlet pressure $p_3 = p_2 - \Delta p_{2-3} = 4.29 \text{ bar}$
7. Assumption: air $c_{p_t} = 1.14 \text{ kJ/kgK}$ (so: $k_t = 1.34$)
8. Expansion ratio: $\epsilon_t = p_3/p_4 = 4.23$
9. Turbine inlet temperature (TIT): $T_3 = T_4 / (1 - \eta_t + \eta_t / \epsilon_t^{\theta_t}) = 1226.31 \text{ K}$
10. Assumption: air $c_{p_{a_{ht}}} = 1.15 \text{ kJ/kgK}$
11. Fuel (fuel h neglected): $m_f = [m_a * c_{p_{a_{ht}}} * (T_3 - T_5)] / (\text{LHV} * \eta_b) = 6.9 \text{ g/s}$
12. Calculation of turbine power: $P_c = (m_a + m_f) * c_{p_t} * (T_3 - T_4) = 283.47 \text{ kW}$
13. Calculation of mechanical power: $P_m = (P_c - P_c) * \eta_m = 111.87 \text{ kW}$
14. Calculation of net electrical power: $P_e = P_m * \eta_e - P_{aux} = 100.00 \text{ kW}$
15. Calculation of machine electrical efficiency: $\eta_g = P_e / (m_f * \text{LHV}) = 0.30$
16. Calculation of exhaust temperature: $T_7 = T_w + \Delta T_{7-W} = 115^\circ\text{C}$
17. Assumption: air $c_{p_{a_{rec}}} = 1.09 \text{ kJ/kgK}$
18. Rec. out. (hot): $T_6 = T_4 - [m_a * c_{p_{a_{rec}}} * (T_5 - T_2)] / [(m_a + m_f) * c_{p_t}] = 567.90 \text{ K}$

Solution (2/2):

19. Calculation of thermal power: $P_{th} = (m_a + m_f) * c_{p,t} * (T_6 - T_7) * \eta_{sc} = 157.1 \text{ kW}$
 20. Calculation of total efficiency: $\eta_{total} = (P_e + P_{th}) / (m_f * LHV) = 0.776$

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